# Basketball Backstop

#### <u>Team 47</u>

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## Motivation and Objectives





## Structure Description

Rear Braced Ceiling-Mounted Basketball Hoop

Front View	216.00 000 000 000 000 000 000 000
	Ceiling Mount
00°912 Top View	T2.00
	Backboard

#### Structural Analysis

Rear Braced Ceiling-Mounted Basketball Hoop

- Completed via determination of stress and displacement values
  - Displacement and Reaction Forces used
  - Conducted at each joint (node) in the Truss
    System
- All Members are assumed to behave as typical bar elements
  - Elastic Modulus, E
  - > Area, A
  - o Length, L
- Stiffness Matrices for individual members are to be combined into full matrix for the truss

$$\mathbf{K} = \frac{EA}{L} \begin{bmatrix} c_x^2 & c_x c_y & c_x c_z & -c_x^2 & -c_x c_y & -c_x c_z \\ c_x c_y & c_y^2 & c_y c_z & -c_x c_y & -c_y^2 & -c_y c_z \\ c_x c_z & c_y c_z & c_x^2 & -c_x c_z & -c_y c_z & -c_z^2 \\ -c_x^2 & -c_x c_y & -c_x c_z & c_x^2 & c_x c_y & c_x c_z \\ -c_x c_y & -c_y^2 & -c_y c_z & c_x c_y & c_y^2 & c_y c_z \\ -c_x c_z & -c_y c_z & -c_z^2 & c_x c_z & c_y c_z & c_z^2 \end{bmatrix}$$

$$C_x = \frac{x_2 - x_1}{L}; C_y = \frac{y_2 - y_1}{L}; C_z = \frac{z_2 - z_1}{L}$$

 Boundary Conditions applied at specific nodes depending on placement and mounting with respect to environment

#### Failure Criteria

Deflection Criteria Applied to the Contact Point Between the Backboard & Truss to Determine System Failure

- Analyze truss system to determine stress and displacement values at different joints (nodes).
   Multiply displacement value with desired factor of safety to obtain failure criteria under deflection.
- $||v_{y_n}|| \le U^*$  n=member #,  $\phi$  =safety factor,  $U_{y_n}$ =deflection at member, U\*=failure value
- Ideal factor of safety for basketball backstops = 55
- The displacement value will be in terms of load applied, area of the beam, elastic modulus of the beam material, and length of the beam.
- Plug in the values including the load to determine if the beam will fail using the inequality.
- Obtain maximum strain value before deformation and multiply length of member, and compare



#### Failure Criteria

Buckling and Yield Criteria Applied to Truss System

- If applied axial load is negative (compression) yielding & buckling must be considered. If positive (tension), only yielding will be considered.
- Multiply the obtained stress value at the nodes with a factor of safety of 55
- Determine if member will buckle or yield after plugging in force, cross-sectional area of the beam, FOS, and comparing against material yield strength.

 $|\phi_{\sigma}|\sigma_n| \leq \sigma^*$  mer

n=member #,  $\phi$  =safety factor,  $\sigma_n$ =stress at member,  $\sigma^*$ =max yield strength



## Minimum Mass Design

In Terms of the Dimensions of Structural Members and the Materials Used We'll have the most control over cross-section area, which we solve using failure criteria. From there, find the mass using:

m = ρ\*A\*L (A and L may vary for each member)

Furthermore, we can minimize the mass by selecting materials according to density.



#### \*Results

- Expectations: All members of the truss system will be in tension as a result of the player interacting with the rim from dunking - this could cause failure by deflection, buckling or yielding to an allowable limit that is yet to be calculated.
- Calculations from the previous slides mentioned would be solved and compared to either support or defer this claim.





Our concluding remarks will summarize our findings detailing any important calculations that led to a change in the system.



